

**Note:** All questions are compulsory.

**Question 1(6 Marks)**

- a. Under the Hungarian Assignment Method, the prerequisite to assign any job is that each row and column must have a zero value in its corresponding cells. If any row or column does not have any zero value then to obtain zero value, each cell values in the row or column is subtracted by the corresponding minimum cell value of respective rows or columns by performing row or column operation. This means *if any row or column have two or more cells having same minimum value then these row or column will have more than one zero*. However, having two zeros does not necessarily imply two equal values in the original assignment matrix just before row and column operations. Two zeroes in a same row can also be possible by two different operations i.e. one zero from row operation and one zero from column operation. **(3 marks)**
- b. The order of matrix in the assignment problem is  $4 \times 4$ . The total assignment (allocations) will be four. In the assignment problem when any allocation is made in any cell then the corresponding row and column become unavailable for further allocation. Hence, these corresponding row and column are crossed mark to show unavailability. In the given assignment matrix two allocations have been made in A24 (2<sup>nd</sup> row and 4<sup>th</sup> column) and A32 (3<sup>rd</sup> row and 2<sup>nd</sup> column). This implies that 2<sup>nd</sup> and 3<sup>rd</sup> row and 2<sup>nd</sup> and 4<sup>th</sup> column are unavailable for further allocation. Therefore, the other allocations are at either at **A11 and A43** or at **A13 and A41**. **(3 marks)**

**Question 2( 8 Marks)**

The Initial basic solution worked out by the shipping clerk is as follows-

Warehous e	Market				Suppl y
	I	II	III	IV	
A	5	2 <b>12</b>	4 <b>1</b>	3 <b>9</b>	22
B	4	8	1 <b>15</b>	6	15
C	4 <b>7</b>	6	7 <b>1</b>	5	8
<b>Req.</b>	7	12	17	9	45

The initial solution is tested for optimality. The total number of independent allocations is 6 which is equal to the desired  $(m + n - 1)$  allocations. We introduce  $u_i$ 's ( $i = 1, 2, 3$ ) and  $v_j$ 's ( $j = 1, 2, 3, 4$ ). Let us assume  $u_1 = 0$ , remaining  $u_i$ 's and  $v_j$ 's are calculated as below-

**( $u_i + v_j$ ) Matrix for Allocated / Unallocated Cells**

					$u_i$
	1	2	4	3	0
	-2	-1	1	0	-3
	4	5	7	6	3
$v_j$	1	2	4	3	

Now we calculate  $\Delta_{ij} = C_{ij} - (u_i + v_j)$  for non-basic cells which are given in the table below-

**$\Delta_{ij}$  Matrix**

4			
6	9		6
	1		-1

Since one of the  $\Delta_{ij}$ 's is negative, the schedule worked out by the clerk is **not the optimal solution**.

**(1 mark)**

**(ii)** Introduce in the cell with negative  $\Delta_{ij}$  [ $R_3C_4$ ], an assignment. The reallocation is done as follows-

	12	1	9
		+1	-1
		15	
7		1	
		-1	+1

**Revised Allocation Table**

	12	2	8
		15	
7			1

Now we test the above improved initial solution for optimality-

**( $u_i + v_j$ ) Matrix for Allocated / Unallocated Cells**

					$u_i$
	2	2	4	3	0
	-1	-1	1	0	-3
	4	4	6	5	2
$v_j$	2	2	4	3	

Now we calculate  $\Delta_{ij} = C_{ij} - (u_i + v_j)$  for non-basic cells which are given in the table below-

$\Delta_{ij}$  Matrix

3			
5	9		6
	2	1	

Since all  $\Delta_{ij}$  for non-basic cells are positive, the solution as calculated in the above table is the optimal solution. (2 Marks)

The supply of units from each warehouse to markets, along with the transportation cost is given below- (1 Mark)

Warehouse	Market	Units	Cost per unit (₹)	Total Cost (₹)
A	II	12	2	24
A	III	2	4	8
A	IV	8	3	24
B	III	15	1	15
C	I	7	4	28
C	IV	1	5	5
<b>Minimum Total Shipping Cost</b>				<b>104</b>

- (a) If the clerk wants to consider the carrier of route C to II only, instead of 7 units to I and 1 unit to IV, it will involve shifting of 7 units from (A, II) to (A, I) and 1 unit to (A, IV) which results in the following table- (2 marks)

Warehouse	Market				Supply
	I	II	III	IV	
A	5	7	2	4	22
B	4	8	1	15	15
C	4	6	8	7	8
Req.	7	12	17	9	45

The transportation cost will become- (1 mark)

Warehouse	Market	Units	Cost per unit (₹)	Total Cost (₹)
A	I	7	5	35
A	II	4	2	8
A	III	2	4	8
A	IV	9	3	27
B	III	15	1	15
C	II	8	6	48
<b>Minimum Total Shipping Cost</b>				<b>141</b>

The total shipping cost will be `141. Additional  
Transportation Cost `37.

The carrier of C to II must reduce the cost by `4.63 (`37/8) so that the total cost of transportation remains the same and clerk can give him business. (1 mark)

**Question 3(4 Marks) (1 mark for each)**

Situation		Appropriate pricing Policy
(i)	'W' is a new product for the company and the market and meant for large scale production and long term survival in the market. Demand is expected to be elastic.	Penetration Pricing
(ii)	'X' is a new product for the company, but not for the market. X's success is crucial for the company's survival in the long term.	Market Price or Price just below market price
(iii)	'Y' is a new product to the company and the market. It has an inelastic market. There needs to be an assured profit to cover high initial costs and the unusual sources of capital have uncertainties blocking them.	Skimming Pricing
(iv)	'Z' is a perishable item, with more than 80% of its shelf life over.	Any Cash Realizable value*

(\* this amount decreases every passing day)

**Question 4(8 Marks)**

Let the P<sub>1</sub>, P<sub>2</sub> and P<sub>3</sub> be the three products to be manufactured. Then the data are as follows:

Products	Product ingredients			Inert Ingredients
	A	B	C	
P <sub>1</sub>	5 %	10%	5%	80%
P <sub>2</sub>	5%	5%	10%	80%
P <sub>3</sub>	20%	5%	10%	65%
Cost per kg ( ` )	64	16	40	16

**Cost of Product P<sub>1</sub>**

$$= 5\% \times `64 + 10\% \times `16 + 5\% \times `40 + 80\% \times `16 = `19.60 \text{ per kg}$$

**Cost of Product P<sub>2</sub>**

$$= 5\% \times `64 + 5\% \times `16 + 10\% \times `40 + 80\% \times `16$$

$$= `20.80 \text{ per kg.}$$

**Cost of Product P<sub>3</sub>**

$$= 20\% \times `64 + 5\% \times `16 + 10\% \times `40 + 65\% \times `16$$

$$= `28.00 \text{ per kg.}$$

Let x<sub>1</sub>, x<sub>2</sub>, and x<sub>3</sub> be the quantity (in kg) of P<sub>1</sub>, P<sub>2</sub>, and P<sub>3</sub> respectively to be manufactured. The LP problem can be formulated:

**Objective function: (2 marks)**

$$\text{Maximize } Z = (\text{Selling Price} - \text{Cost Price}) \times \text{Quantity of Product}$$

$$= (`32.60 - `19.60) x_1 + (`34.80 - `20.80) x_2 + (`36.00 - `28) x_3$$

$$= 13x_1 + 14x_2 + 8x_3$$

**Subject to Constraints: (6 marks)**

$$1/20x_1 + 1/20x_2 + 1/5x_3 \leq 100$$

Or  $x_1 + x_2 + 4x_3 \leq 2,000$

$$1/10x_1 + 1/20x_2 + 1/20x_3 \leq 180$$
  

Or  $2x_1 + x_2 + x_3 \leq 3,600$

$$1/20 x_1 + 1/10 x_2 + 1/10 x_3 \leq 120$$

Or  $x_1 + 2x_2 + 2x_3 \leq 2,400$

$$x_1 \leq 30$$

and  $x_1, x_2, x_3 \geq 0$

**Question 5 (10 Marks)**

**Statement Showing Impact on Airline's Profit if Flight Y-09 is Discontinued (5 marks)**

Contribution Margin lost if the flight is discontinued		-784000
Less: <u>Flight Costs which can be avoided if the flight is discontinued:</u>		
Flight Promotion	35000	
Fuel for Aircraft	255000	
Liability Insurance (1/3 x `1,53,000)	51000	
Salaries, Flight Assistants	45500	
Overnight Costs for Flight Crew and Assistants	18000	404500
		-379500

If Aves Airlines Ltd. goes for discontinuation of flight K-09, its profit will go down by `3,79,500.

Following costs are **not relevant** to the decision: (5 marks)

- Salaries, flight crew - Fixed annual salaries which will not change
- Baggage loading and flight preparation- This is an allocated cost, which will continue even if the flight is discontinued.
- Depreciation of aircraft -Sunk Cost
- Liability insurance (two third)
- Hanger parking fee- This cost will be incurred regardless of whether the flight is made.

**Question 6 (6 Marks)**

**Statement Showing "Cost and Profit for the Next Year" (4 marks)**

Particulars	Existing Volume, etc.	Volume, Costs, etc. after 10% Increase	Estimated Sale, Cost, Profit, etc.*
	(`)	(`)	(`)
Sale	5,00,000	5,50,000	5,72,000
Less: Direct Materials	2,50,000	2,75,000	2,69,500
Direct Labour	1,00,000	1,10,000	1,07,800
Variable Overheads	40,000	44,000	43,120
Contribution	1,10,000	1,21,000	1,51,580
Less: Fixed Cost#	60,000	60,000	58,800
Profit	50,000	61,000	92,780

(\*) for the next year after increase in selling price @ 4% and overall cost reduction by 2%.

(#) Fixed Cost = Existing Sales – Existing Marginal Cost – 12.5% on `4,00,000  
 = `5,00,000 – `3,90,000 – `50,000  
 = `60,000

Percentage Profit on Capital Employed equals to 23.19% (92,780/400,000\*100) (1 mark)

Since the Profit of ₹2,780 is more than 23% of capital employed, the proposal of the Sales Manager can be adopted. (1 mark)

**Question 7 ( 8 Marks)**

**Preparation of Production Cost Budget for 50,000 units for the year 2014 (4 Marks)**

Particulars	Cost Per Unit	Total Amount (₹)
Materials (W.N.-1)	1.645	82,237.50
Wages (W.N.-2)	1.43	71,500.00
Variable Overhead	0.50	25,000.00
Fixed Overhead (₹35,000 × 110%)	0.77	38,500.00
Total Cost	4.345 (Approx.)	2,17,237.50

**Working Notes**

**1. Material Cost- (2 Marks)**

(a) Increase in Material Price in the Year 2013-

$$= \frac{\text{Actual Cost per unit in 2013} - \text{Budgeted Cost per unit in 2013}}{\text{Budgeted Cost per unit in 2013}} \times 100$$

$$= \frac{\frac{₹ 53,750}{43,000 \text{ units}} - ₹ 1}{₹ 1} \times 100$$

$$= 25\%$$

(c) Material Required to Produce 50,000 units-

$$= \frac{42,000 \text{ units}}{39,900 \text{ units}} \times 50,000 \text{ units}$$

$$= 52,632 \text{ units (rounded)}$$

(d) Increased Cost for 50,000 units in the Year 2014-

$$= \frac{₹ 53,750}{43,000 \text{ units}} \times 125\% \times 52,632$$

$$₹ 82,237.50$$

**Wages- (2 Marks)**

Rate per hour in 2014-

$$\frac{\text{Wages Paid in the Year 2013}}{\text{Actual Units Produced}} + ₹ 0.20$$

$$= \frac{₹ 44,660}{40,600 \text{ units}} + ₹ 0.20$$

$$= ₹ 1.30$$

(b) Wages to be paid for 50,000 units i.e. for 50,000 hours (1 hour per unit). When the labour efficiency is 90% only, then Total Wages will be-

$$= 50,000 \text{ hours} \times \frac{110}{100} \times ₹ 1.30$$

$$= ₹ 71,500$$

*Note: **Fixed Overhead** can also be calculated on the basis of previous year's budgeted figure.  
**Variable Overhead** may also be calculated by taking ` 1 per unit.  
This question can also be solve by taking 50,000 hrs. as 90% of total hrs. required to produce the 50,000 units.*

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